

## NUMERICAL MODELING OF OPEN PIT (OP) TO UNDERGROUND (UG) TRANSITION IN COAL MINING

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**Abstract:** The primary objective of the present paper is an attempt at evaluating the influence of sub-level caving operations on the slope stability of a still-functioning open pit coal mine in Vietnam. Initially, various methods of predicting the impact of underground mining on surface stability are discussed. Those theoretical considerations were later utilized in the process of constructing a Flac-2D-software-based numerical model for calculating the influence of underground operation on the deformation and possible loss of stability of an open pit slope. The numerical analysis proved that the values of open pit slope displacements were affected mainly by underground exploitation depth, direction of operation (i.e., from one slope to the other) and the distance from the slope plane. Real geomechanical strata parameters from the Vietnamese coal basin of Cam Pha were used in the modeling process. The paper is, therefore, a critical review of the hitherto proposed methods of predicting the impact of underground operation (UG) on open pit mining (OP), illustrated with selected examples of case studies on OP-UG interaction, followed by an original experiment based on numerical modeling method. This is first such study for the genuine conditions of the coal mining in Vietnam. The obtained results, however, should not be generalized due to a highly specific character of the analyzed phenomenon of mining-induced surface deformation. The practical implications of the study may occur extremely useful in the case of an UG-OP transition. Such a transition is often necessary for both technical and economical reasons, as in some coal basins open pit operations at greater depths occur unfeasible, which calls for a proper selection of parameters for a planned underground operation.

*Key words: coal mining, numerical modeling, transition from OP to UG, surface deformation*

### 1. INTRODUCTION

A dynamic development of civilization results in a highly increased demand for natural resources. It applies to almost all types of resources, such as: en-

ergy resources, metals and rock minerals. In the case of open pit mines or underground mines, their operation is nowadays being run at constantly increasing depths, whereas in the case of open pit mines, further increase of exploitation depth proves impossible due to economic and technological limitations, as well

Table 1. Overview of major historical and future OP-UG transitions for ore body mining (modified after Visser [27])

Country	Mine name	Company	Transition year	Main product
Australia	Argyle	Rio Tinto	2010	Diamonds
	Fosterville	Perseverance	2006	Gold
Canada	Kidd Creek	Falconbridge	1973	Copper, Nickel
	Stobie	Inco	1948	Copper, Nickel
Chile	Chuquicamata	Codelco	2019	Copper
	Mansa Mina	Codelco	2020	Copper
Indonesia	Grasberg	Rio Tinto	2017	Copper, Gold
Russia	Mir	Alrosa	2001	Diamonds
	Udachny	Alrosa	2010	Diamonds
South Africa	Finsch	DeBeers	1990	Diamonds
	Palabora	Rio Tinto	2001	Copper
	Venetia	DeBeers	2021	Diamonds
Sweden	Kiruna	LKAB	1958	Iron
USA	Bingham Canyon	Rio Tinto	2018	Copper

as safety measures. Moreover, many mines constitute a significant part of the regional or country economy. Liquidating those mines would have negative national economic implications, such as loss of tax income and increased dependence on foreign resources (Visser [27]). This situation also takes place in some open pit coal mines in Vietnam, which are planning to change the exploitation method. In the mining world, for a number of reasons, the size of mining operations considering an OP-UG transition is strongly increasing (Table 1). In the decision-making process, various factors should be taken under consideration. One of them is an assessment of the impact of underground mining on the stability of pit slopes.

## 2. SURFACE SUBSIDENCE PREDICTION

Generally, after any mineral exploitation, the breach of the structure of the rock mass will occur with distinctive features, depending on the method of underground exploitation (Fig. 1 and Fig. 2). In the case of longwall methods for coal exploitation, there are three zones: caved zone, fractured zone and sagging zone, which will appear above coal seam after exploitation (Fig. 1). A number of empirical formulas were developed in order to determine the impact of these zones on the volume of surface subsidence: Znański [33], Lisowski [14], Ropski [22], Sałustowicz [23], Staroń [25], Peng and Chiang [19], Peng [19], Bai et al. [2], Mazurkiewicz et al. [15].

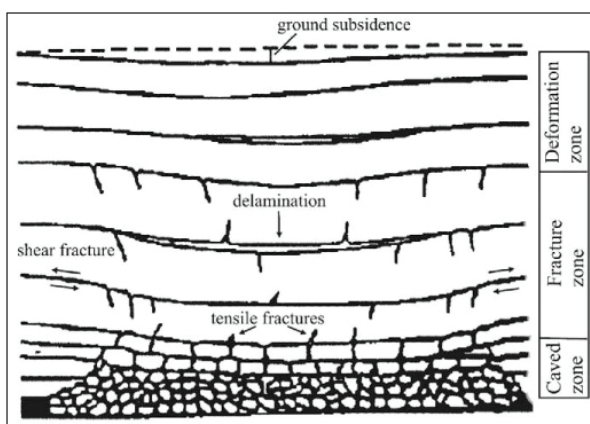


Fig. 1. Caved zone, fractured zone and sagging zone formed after exploitation of a longwall coal-mining panel (after Peng and Chiang [19])

Over the years, many theories were also developed in order to predict mining-induced surface deformation. Further details on the subject can be found, inter alia, in the following works: Gonot (1858), Dumont

(1871), Fayol (1885), Halbaum (1903), Schmitz (1923), Keinhorst (1925), Bals (1931). In the following years, Bals' method was supplemented and modified by various researchers, mostly by German authors. Bals' ideas were developed in the fullest form of geometrical integral theories by Polish researchers in the 1950's (Knothe [11]; Budryk [4]; Kochmański [13]).

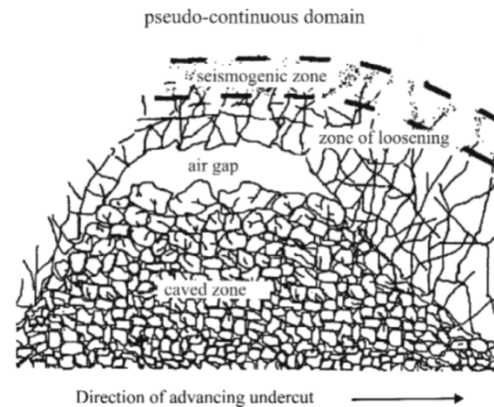


Fig. 2. Conceptual model of caving (after Duplancic and Brady [6])

Based on the theory of Knothe [11], [12], the concept of determining the range of influences, called "the radius of main influences"  $r(z)$ , was published by Piwowarski et al. [21]. In late 1990's, Xueyi Yu presented a method based on the theory of Knothe to predict displacements and deformations in mountainous areas for coal mining conditions in China (Yu [32]).

In mining practice, most commonly used methods to predict the surface deformation are geometrical-integral methods, based on the influences functions describing the shape of the trough. The methods of surface deformation prediction are effective for horizontal or almost horizontal areas, as well as for one single coal seam operation. However, surface deformation prediction is much more difficult for the operation of multi coal seams and complex topography.

In addition, empirical methods fail to characterize the interaction between layers of rocks, hence they do not allow taking into account a number of factors (i.e., factors related to geological structure, rock mass properties, the presence of discontinuities and underground water). Each mine is characterized by a unique combination of geological and mining conditions. Ignoring geotechnical factors may lead to conditions of high risk and thus result in loss of material, equipment and/or personnel. Hence, the prediction of the impact of underground mining on slope surface by using analytical or empirical methods proves unsatisfactory for a comprehensive analysis of subsidence/deformation prediction.

Table 2. Numerical studies of caving-induced surface subsidence (Vyazmensky [28])

Authors	Code	Type of analysis
Singh et al. (1993)	FLAC 2D	Rajpura Daribaand Kiruna
Karzulovic et al. (1999)	FLAC 2D	El Teniente
Van As (2003)	FLAC 3D	Northparkes
Cavieres et al. (2003)	3DEC	El Teniente
Flores and Karzulovic (2004)	FLAC 2D and FLAC 3D	Conceptual
Gilbride et al. (2005)	PFC 3D	Questa
Brummer et al. (2006)	3DEC	Palabora
Elmo et al. (2007)	FLAC 3D	San Manuel
Villegas & Nordlund (2008)	Phase2, PFC 2D	Kiruna

In recent years, with the development of computer science, numerical methods become more and more popular in solving problems of geo-engineering. They prove particularly useful when their results are used for comparison with the results of observations under natural conditions. Issues related to displacement and surface deformation predictions are also solved by means of applying numerical methods.

For ore-body mining using underground method of “caving”, the most important works in the field of surface deformation prediction are presented in Table 2.

In Poland, the implementation of numerical methods for surface deformation prediction in coal mining using the “longwall” underground method was presented by Kwaśniewski and Wang [10], Tajduś [26], Florkowska [7], Wesołowski et al. [29] and Wesołowski [30]. In his work, Tajduś performed an analysis for dozens of models: linear-elastic, non-linear-elastic, elastic-plastic, and compared the results with the results obtained from Knothe’s theory. He argued that with suitable properties for “transversally isotropic” numerical model, surface displacements obtained are close to the results measured under natural conditions. The study was carried out with the use of finite element method (FEM). Wesołowski, by means of the appropriate selection of properties for a transversally isotropic model, also obtained results consistent with Knothe’s theory. The research was performed with the application of finite difference method (FDM) using FLAC 3D code.

### 3. CASE STUDIES ON UG-OP INTERACTION

Mining activity is one of the most important factors affecting the change of natural phenomena in the rock mass. Underground operation causes subsidence, slope movements, discontinuous deformations and

change of hydrogeological conditions. In the case of underground operation located below the open pit mine, slope strain can be expected as a result of subsidence induced by underground exploitation. Changes in physical and mechanical properties of rock mass, groundwater levels and the state of stress inside the slope can lead to slope deformation.

#### *Enormous disaster at the mine Palabora, South Africa*

Palabora mine is one of the steepest and deepest large open pits in the world, with a radius of about 1.5 km, and a depth of about 800 m. The transition from open pit to block caving embraced extracting a 400 m column below the pit floor (Fig. 3). The geology of the mine (a volcanic plug) is extremely complex. Besides various rock types (up to ten types at the mine) with different properties, there are four main faults crossing the pit and three dominant joint sets ubiquitous in the mine. Ground water is also present (Brummer et al. [3]).

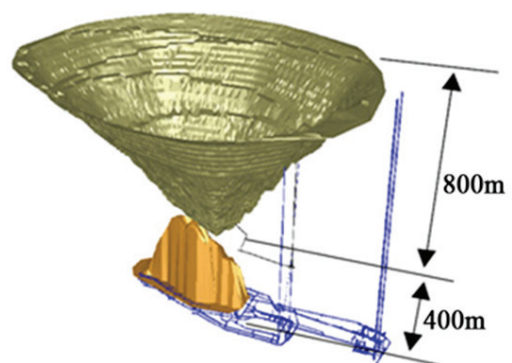


Fig. 3. Three-dimensional model of pit and cave at Palabora mine (Brummer et al. [3])

Seismic monitoring data indicates that the crown pillar failed in April 2004 with the cave breaking through to the open pit. Subsequent to this was a ma-



major open pit wall failure that occurred in September 2004. The failure dimensions were some 800 m in height by 300 m along the wall, with the crest of approx. 50 m back from the pit rim. Nearly 130 million tons of waste filled the North-West corner and the floor of the open pit (Fig. 4). A physical model was constructed in 2005 and the impact of waste material on the ore reserves was quantified with the use of Rebob (particle flow simulation software). Results indicated that there would be approximately 30 per cent of ore reserve loss (Ngidi and Boshoff [18]).



Fig. 4. Failure at Palabora mine (modified after Ngidi and Boshoff [18])

In order to determine the phenomena occurring inside the rock mass, which led to the catastrophe, and predict further damage, many numerical analyses have been carried out, including: Brummer et al. [3]; Moss et al. [16]; Vyazmensky [28]; Severini et al. [24]; Woo et al. [31]; Ngidi et al. [18]; Ahmed et al. [1].

#### *Sublevel caving and open pit interaction at the Ernest Henry mine, Australia*

At the Ernest Henry mine, the open pit operated to 2011 and had its final dimensions of 1.5 km by 1.3 km at a 530 m depth. Sublevel caving production began after completion of the open pit with the planned cave footprint of a 220 m column (Fig. 5).

Pit failure started to occur after the pillar had been removed and the initial sublevel had been completed in late 2012. A large collapse occurred in December 2014 (Fig. 6). From laser scanning, the estimated volume was 935,000 m<sup>3</sup> (about 2.5 Mt of rock). The failure dimensions measured about 200 m wide, 150 m high and 30 m thick. More details about this case can be found in the study of Campbell et al. [5].

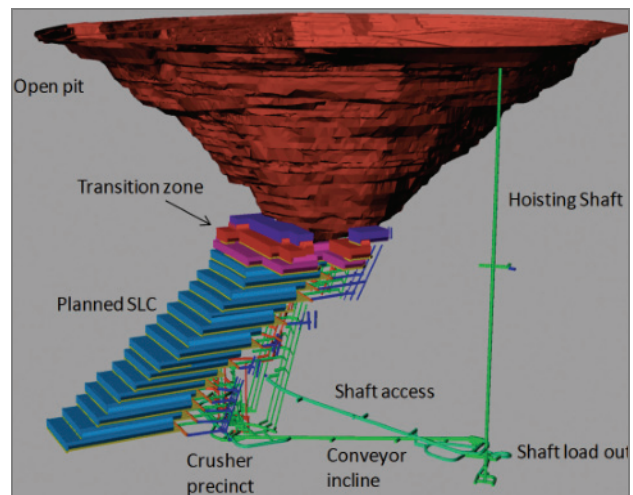


Fig. 5. Three dimensional view of the sublevel cave and final pit at the Ernest Henry mine (Campbell et al. [5])

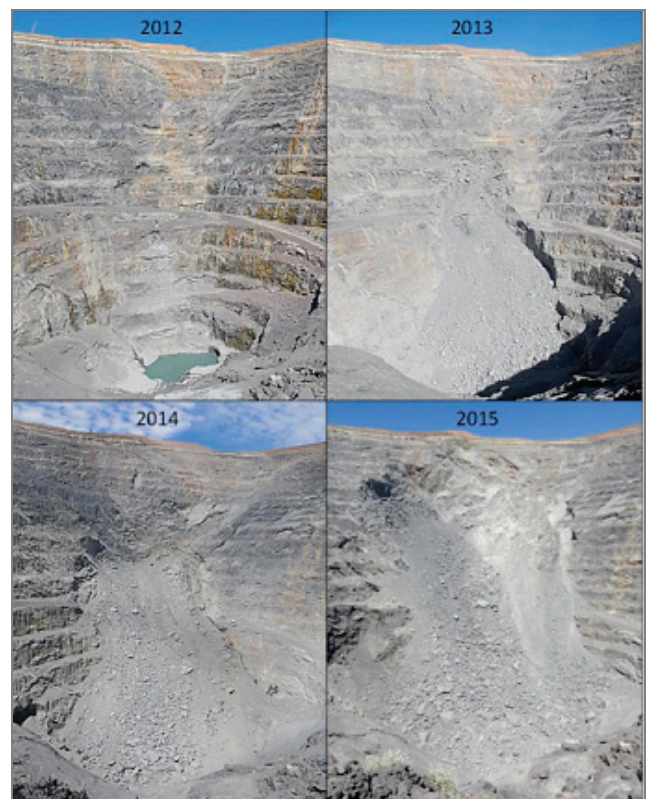


Fig. 6. Progression of caving-induced pit wall failure (Campbell et al. [5])

The examples above seem to provide a clear warning regarding the possible impact of underground mining on open pit mines. Therefore, it is necessary to carry out more research and analysis on slope stability of open pit affected by underground mining. Due to the different geological conditions and the technology application, any such case should be analyzed individually.



$$g^s = \sigma_1 - \sigma_3 N_\psi,$$

$$N_\psi = \frac{1 + \sin \Psi}{1 - \sin \Psi}, \quad (7)$$

where  $\psi$  is the dilation angle.

The associated flow rule for tensile failure is derived from the potential function in the form

$$g^t = -\sigma_3. \quad (8)$$

The flow rules for this model are given a unique definition in the vicinity of the edge of the composite yield function in three dimensional stress space for the case of shear-tension edge. The function is presented by the diagonal between the presentation of shear yield function and tension yield function in the plane  $(\sigma_1, \sigma_3)$

$$h = \sigma_3 - \sigma^t + \alpha^p (\sigma_1 - \sigma^p),$$

$$\alpha^p = \sqrt{1 + N_\theta^2} + N_\theta, \quad (9)$$

$$\sigma^p = \sigma^t N_\theta - 2c\sqrt{N_\theta}.$$

The flow rule has the form

$$\Delta e_i^p = \lambda^s \frac{\partial g^s}{\partial \sigma_i}; \quad i = 1, 3 \quad (10)$$

where  $\lambda^s$  is an unknown parameter. Using equation (7) for  $g^s$ , these equations become, after partial differentiation,

$$\Delta e_1^p = \lambda^s,$$

$$\Delta e_2^p = 0, \quad (11)$$

$$\Delta e_3^p = -\lambda^s N_\psi.$$

The elastic strain increments may be expressed from equation (2) as total increment minus plastic increment. In further using equation (11), the elastic laws in equation (3) become

$$\Delta \sigma_1 = \alpha_1 \Delta e_1 + \alpha_2 (\Delta e_2 + \Delta e_3) - \lambda^s (\alpha_1 - \alpha_2 N_\psi),$$

$$\Delta \sigma_2 = \alpha_1 \Delta e_2 + \alpha_2 (\Delta e_1 + \Delta e_3) - \lambda^s \alpha_2 (1 - N_\psi), \quad (12)$$

$$\Delta \sigma_3 = \alpha_1 \Delta e_3 + \alpha_2 (\Delta e_1 + \Delta e_2) - \lambda^s (-\alpha_1 N_\psi + \alpha_2).$$

Let the new and old stress states be referred to by the superscripts  $N$  and  $O$ , respectively. Then, by definition

$$\sigma_i^N = \sigma_i^O + \Delta \sigma; \quad i = 1, 3. \quad (13)$$

Substituting equation (12) we may write

$$\sigma_1^N = \sigma_3^I - \lambda^s (\alpha_1 - \alpha_2 N_\psi),$$

$$\sigma_2^N = \sigma_2^I - \lambda^s \alpha_2 (1 - N_\psi), \quad (14)$$

$$\sigma_3^N = \sigma_3^I - \lambda^s (-\alpha_1 N_\psi + \alpha_2),$$

where the superscript  $I$  is used to represent the elastic guess, obtained by adding the old stress elastic increments computed using the total strain increments

$$\sigma_1^I = \sigma_1^O + \alpha_1 \Delta e_1 + \alpha_2 (\Delta e_2 + \Delta e_3),$$

$$\sigma_2^I = \sigma_2^O + \alpha_1 \Delta e_2 + \alpha_2 (\Delta e_1 + \Delta e_3), \quad (15)$$

$$\sigma_3^I = \sigma_3^O + \alpha_1 \Delta e_3 + \alpha_2 (\Delta e_1 + \Delta e_2).$$

The parameter  $\lambda^s$  may now be defined by requiring that the new stress point be located on the shear yield surface

$$\lambda^s = \frac{f^s(\sigma_1^I, \sigma_3^I)}{(\alpha_1 - \alpha_2 N_\psi) - (-\alpha_1 N_\psi + \alpha_2) N_\psi}. \quad (16)$$

In the case of tensile failure, the flow rule has the form

$$\Delta e_i^p = \lambda^t \frac{\partial g^t}{\partial \sigma_i}; \quad i = 1, 3 \quad (17)$$

where  $\lambda^t$  is unknown parameter. Using equation (8) for  $g^t$ , these equations become, after partial differentiation

$$\Delta e_1^p = 0,$$

$$\Delta e_2^p = 0, \quad (18)$$

$$\Delta e_3^p = -\lambda^t.$$

Repeating a reasoning similar to that described above, we obtain

$$\sigma_1^N = \sigma_1^I + \lambda^t \alpha_2,$$

$$\sigma_2^N = \sigma_2^I + \lambda^t \alpha_3, \quad (19)$$

$$\sigma_3^N = \sigma_3^I + \lambda^t \alpha_1,$$

and

$$\lambda^t = \frac{f^t(\sigma_3^I)}{\alpha_1}. \quad (20)$$

These formulas allow the components of the stress state to be determined in each step of the calculation. Knowing the stress we are able to calculate the com-

ponents of the state of displacement in each node of the grid and determine the state of material effort, based on accepted values of strength parameters.

#### 4.2. MODEL DESCRIPTION

Prediction of interaction between UG and OP was carried out with the application of Flac 2D software based on Finite Difference Method (Itasca). All parameters of rock mass used for the modeling are based on laboratory tests for geological and mining conditions of Quang Ninh coal basin in Vietnam (Table 3).

In order to determine the geometry of the model, the heights of the caved zone  $h_{zw}$  and the fractured zone  $h_s$  were calculated. Their mechanical properties are different depending on the rock mass intact and strongly affect the surface deformation shape. These parameters are defined by the formulas below (Kendorski, Roosendaal and Bai [2])

$$h_{zw} = \frac{100g}{c_1g + c_2}, \quad h_s = \frac{100g}{c_2g + c_4} \quad (1)$$

where

$h_{zw}$  – height of caved zone, m;

$h_s$  – height of fractured zone, m;

$g$  – coal bed thickness, m;

$c_1, c_2, c_3, c_4$  – constant coefficients dependent on compressive strength (Table 4).

Rock mass in the basin Cam Pha is classified as strong and hard, so the height of the caved zone is approximately 13 m, while the height of the fractured zone is approximately 53 m, assuming the coal bed thickness of 3.0 m.

Since there is no access to the caved zone and the fractured zone, these zones were assumed as strongly cracked rock and cracked rock. Therefore, deformation and strength parameters were selected according to the investigations of Nawrot [17], which assumed that mechanical parameters of caved zone were 20–40 times lower and mechanical parameters of the fractured zone were 2–3 times lower than the parameters of intact rock located in the roof zone. The parameters of the caved zone and the fractured zone in longwall operation are presented in Table 5 after calibration process by using “back analysis” method and Knothe’s theory. These parameters are dependent on the depth of longwall mining panel.

Table 3. Mechanical parameters of the rock mass used in numerical modeling

Material	Young modulus $E$ [GPa]	Cohesion $c$ [MPa]	Tensile strength $\sigma'$ [MPa]	Friction angle $\theta$ [°]	Poisson ratio $\nu$ [-]	Bulk density $\rho$ [kg/m <sup>3</sup> ]
Roof	1.2	1	0.5	28	0.25	2,600
Coal	1.4	1.2	0.6	30	0.25	1,500
Floor	1.8	1.5	0.75	32	0.25	2,600

Table 4. Coefficients for average height of caved zone and fractured zone (Kendorski, Roosendaal and Bai [2])

Strata lithology	Compressive strength [MPa]	Coefficients			
		$c_1$	$c_2$	$c_3$	$c_4$
Strong and hard	>40	2.1	16	1.2	2
Medium strong	20÷40	4.7	19	1.6	3.6
Soft and weak	<20	6.2	32	3.1	5

Table 5. Mechanical parameters of caved zone and fractured zone

Material	Young’s modulus $E$ [GPa]	Cohesion $c$ [MPa]	Tensile strength $\sigma'$ [MPa]	Friction angle $\theta$ [°]	Poisson’s ratio $\nu$ [-]	Bulk density $\rho$ [kg/m <sup>3</sup> ]
Coal seam is located at 400 m depth below pit crest (case study II)						
Caved zone	0.06	0	0	30	0.3	2,000
Fractured zone	0.6	0.5	0.25	25	0.25	2,600
Coal seam is located at 150 m depth below pit floor (case study III)						
Caved zone	0.03	0	0	10	0.25	2,000
Fractured zone	0.6	0.5	0.25	20	0.25	2,600

Figure 8 shows the dimensions of the numerical model and the location of the caved zone and the fractured zone above the longwall panel. The numerical model consists of 12524 zones and fixed (restrained) bottom and two sides

It was assumed that the rock mass was stratified with the properties according to the elastic-plastic model of Mohr–Coulomb. The initial model was solved as an elastic model in order to obtain the initial stress conditions. Then, the vectors and speeds of displacements were zeroed. The next step was assigning the “null” model to the zone corresponding to the caved zone and the fractured zone, and re-assigning the Mohr–Coulomb model with equivalent parameters to those zones and calculating it again.

Calculations were performed for three variants (cases) (Fig. 8).

- Case I: the coal seam is located at 150 m depth below the pit floor. Location of the longwall panel is changed every 100 m along the horizontal axis. The geometry of the numerical model assumed the following longwall dimensions: 300 m in length and 3 m in height (Fig. 8).
- Case II: the coal seam is located at 400 m depth below the slope crest. Longwall operation proceeds from the left side to the upper edge with the advancement rate of 100 m (Fig. 9).
- Case III: coal seam is located at 150 m depth below pit floor. Long wall operation proceeds from the right side to the lower edge with the advancement rate of 100 m (Fig. 10).

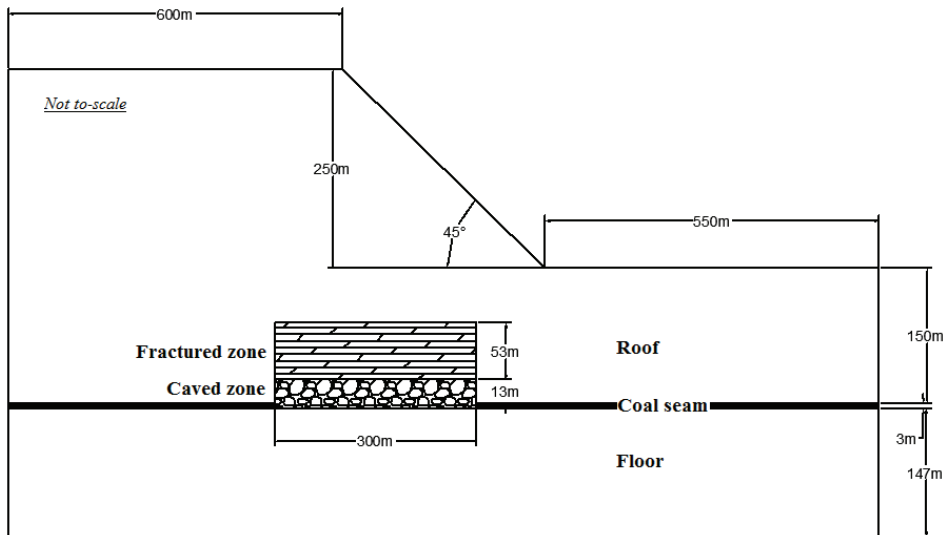


Fig. 8. Two-dimensional numerical model and location of rock layers

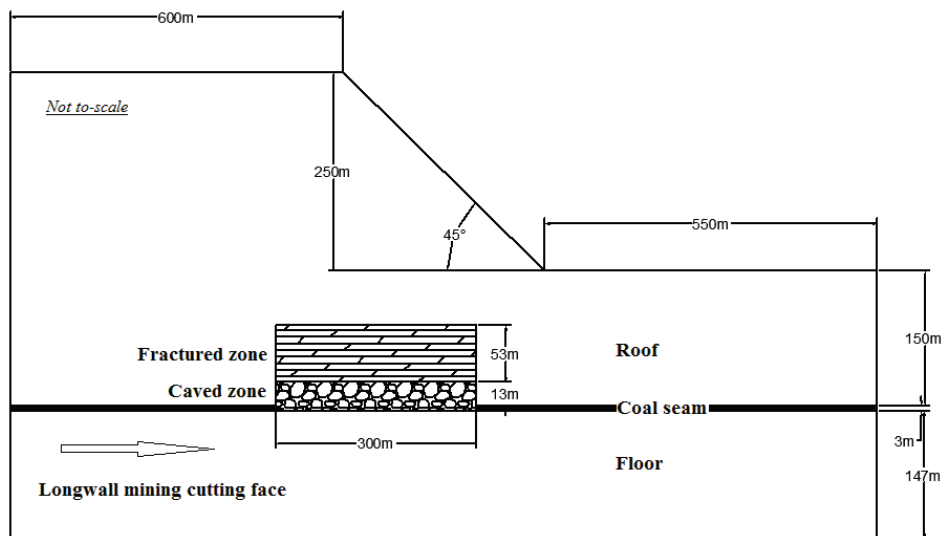


Fig. 9. Two-dimensional numerical model dal case study II



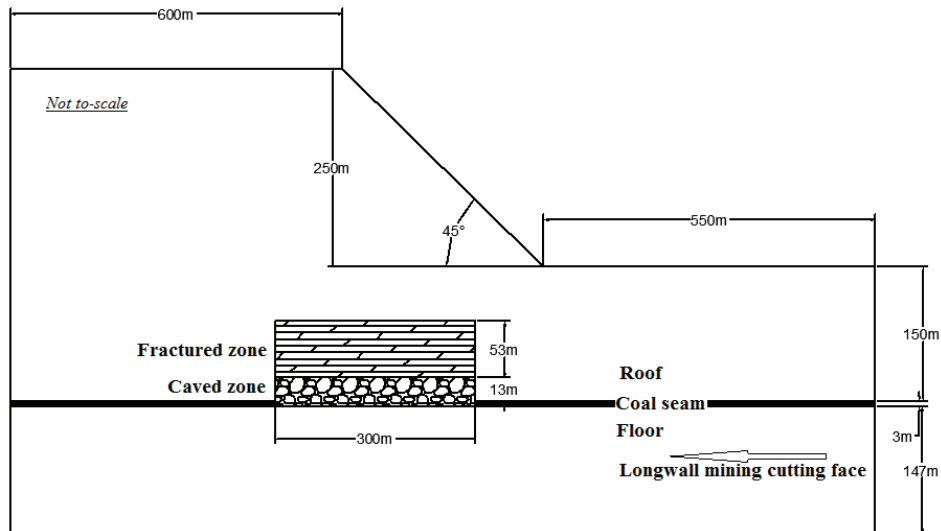


Fig. 10. Two-dimensional numerical model dal case study III.

Note: Speed of exploitation is omitted, only the size of coal extraction has been taken into account.  
Cutting face advanced every 100 m toward open pit slope

### 5. ANALYSIS OF RESULT

The displacements, plasticity and velocity vectors were analyzed in order to assess the impact of underground mining on open pit slope. Slope deformation generated by longwall operation may lead open pit slope to the loss of stability.

**Case I:** The longwall panel is located perpendicularly to the model

For this model the position of the longwall panel changed at a constant depth along the horizontal axis in relation to the open pit slope. Figure 11 shows vertical displacement of the slope face depending on

the position of the longwall panel, wherein the distance measured is the center of the longwall panel. Calculations show that the largest vertical displacements along the slope face can be expected when the center of the longwall panel was located in the range of distances from 150 m before the upper edge to 250 m behind the upper edge. The values of subsidence are in the range from 1.13 to 2.1 m. The horizontal displacements also indicated that, for the above position of the longwall panels, they can be significant up to 1.1 m in the direction of pit slope (Fig. 12). Such movements may be an impulse for the loss of slope stability. This is confirmed by plasticity indicators, which show that slope failures may occur in particular areas (Fig. 13).

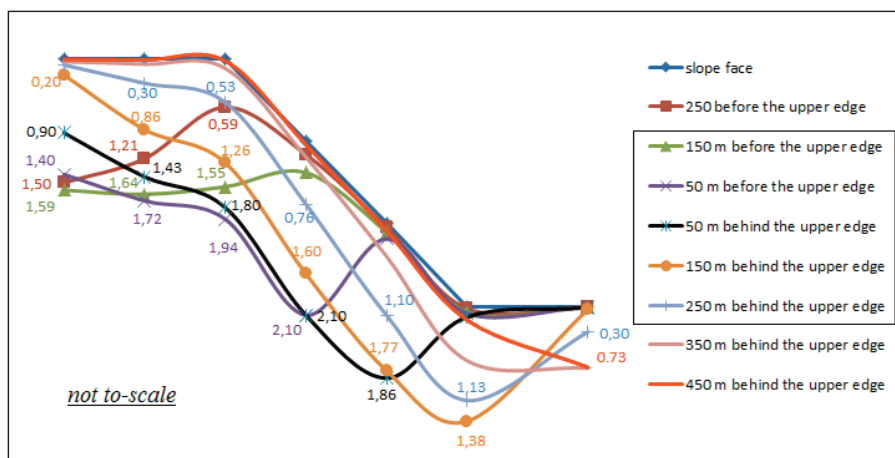


Fig. 11. Vertical displacements of slope face at different positions of longwall panel (measured point is the center of the longwall panel)

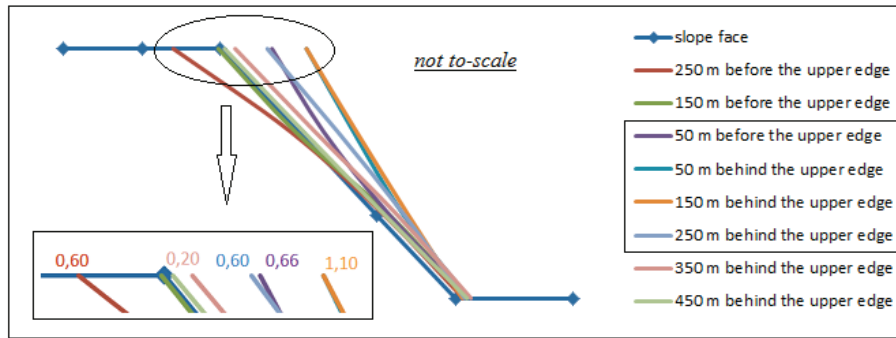


Fig. 12. Horizontal displacements of slope face at different positions of longwall panel (measured point is the center of the longwall panel)

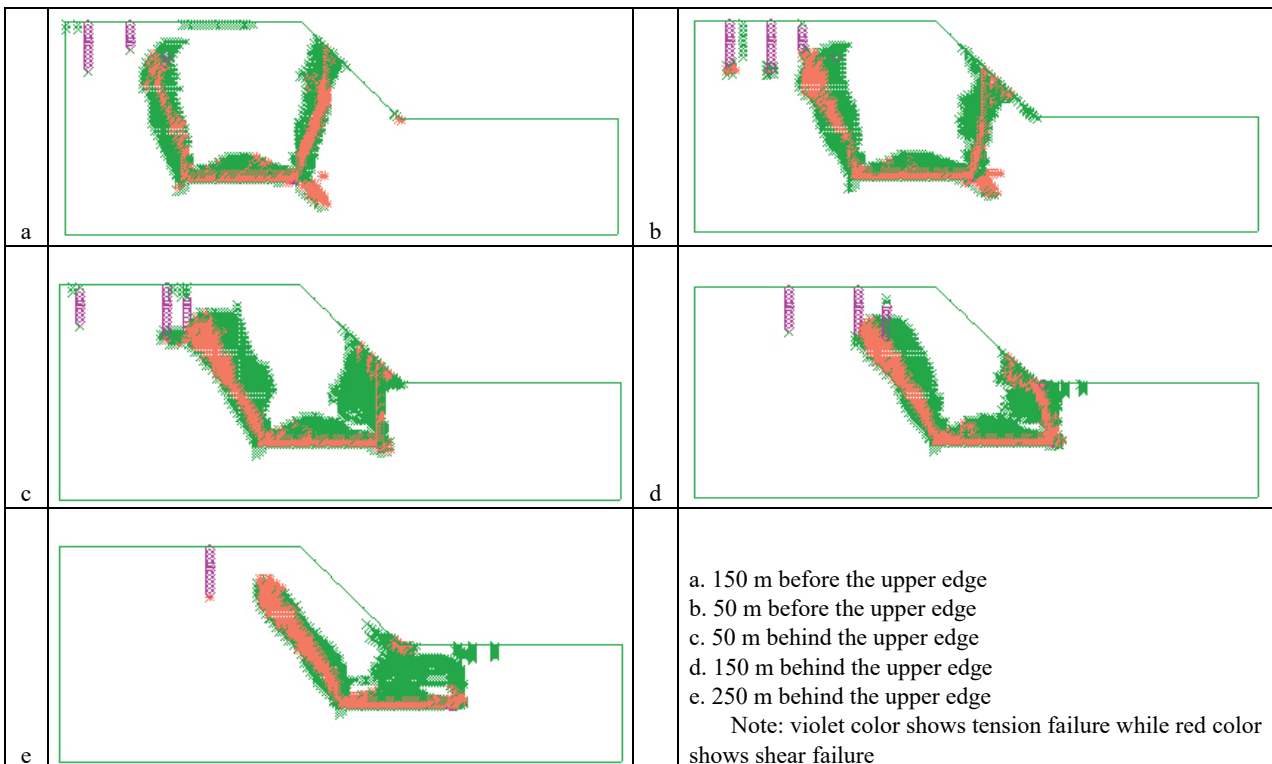


Fig. 13. Plasticity indicator of rock mass at different positions of longwall panel (measured point is the center of the longwall panel)

**Case II:** Longwall operation proceeds from the left side towards the upper edge of the open pit slope

The results calculated for this case indicate that the upper edge starts to move with a large extent when the long wall face reaches the distance of 100 m from the upper edge (Fig. 14). The maximum subsidence of the upper edge and slope occurs when the longwall face reaches 100 m behind the upper edge. Subsidence values are in the range of 1.4÷2.2 m.

Horizontal displacements of Case II reach a value in the range of 0.5÷1.0 m (Fig. 15). In this case, the direction of movements leads to a reduction of the

slope angle, which is advantageous from the point of view of slope stability. However, the displacement can lead to such changes in the properties of rock mass that can cause instability.

The increase of velocity vectors is almost 2 times for the situation when the longwall face is less than 200 m from the upper edge of the slope (Fig. 16c÷e), which indicates the possibility of failure on the slope face. The direction of velocity vectors, as well as the direction of displacement, however, is advantageous from the point of view of slope stability. Nevertheless, it may weaken the rock mass and lead to the loss of slope stability in the future.

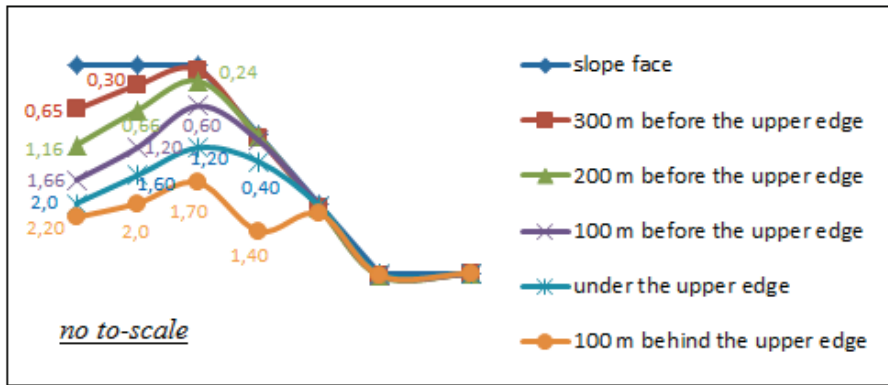


Fig. 14. Vertical displacement of slope face when the longwall operation proceeds from the left side towards the upper edge of slope (measured point is the face of the longwall panel)

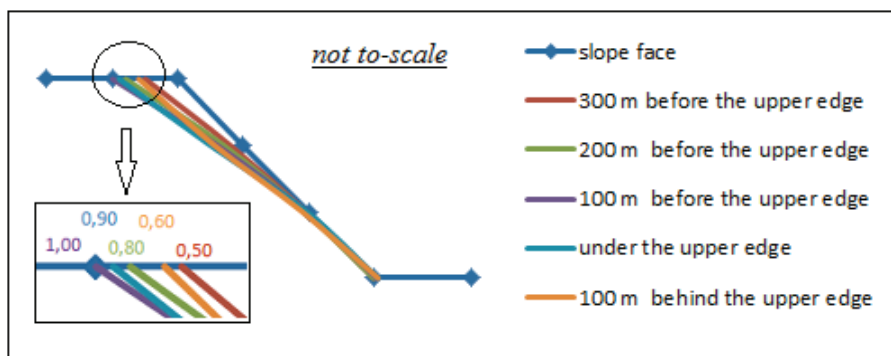
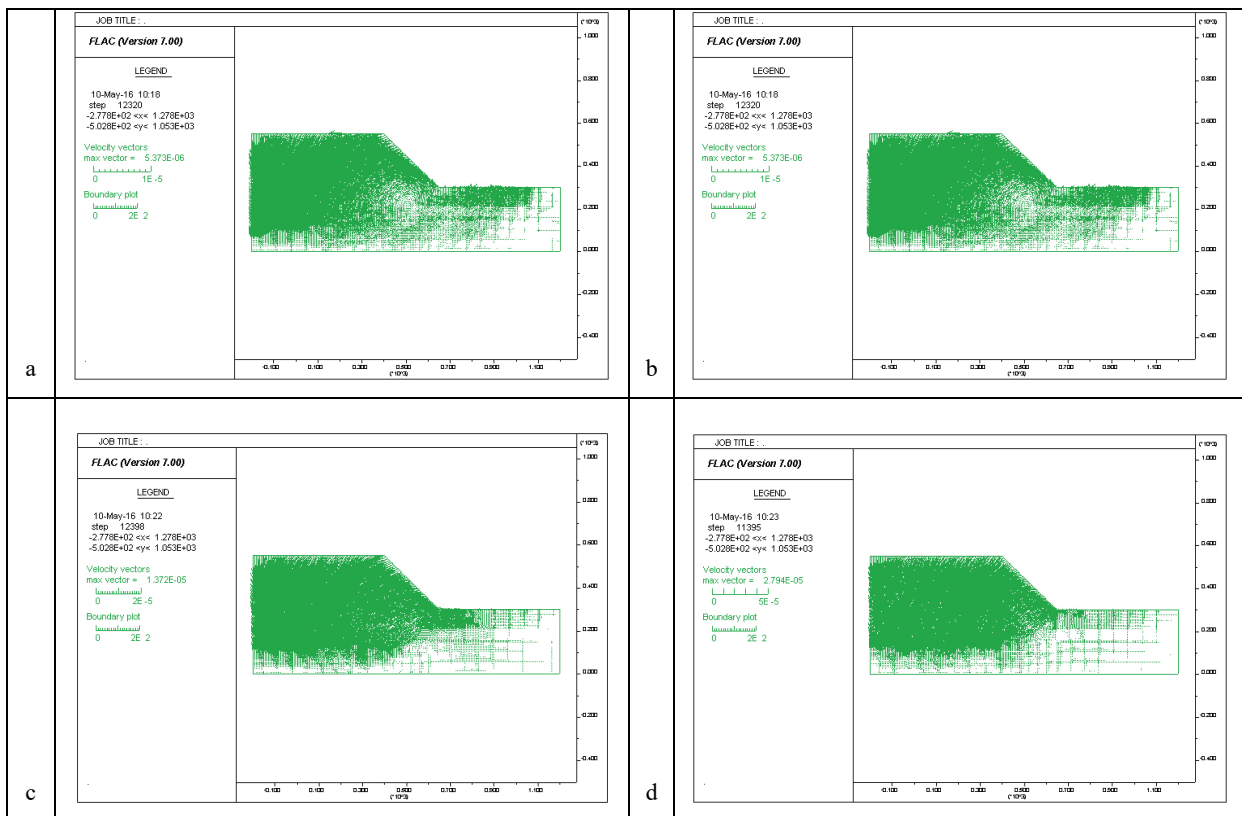


Fig. 15. Horizontal displacement of slope face when the longwall operation proceeds from the left side towards the upper edge of slope (measured point is the face of the longwall panel)



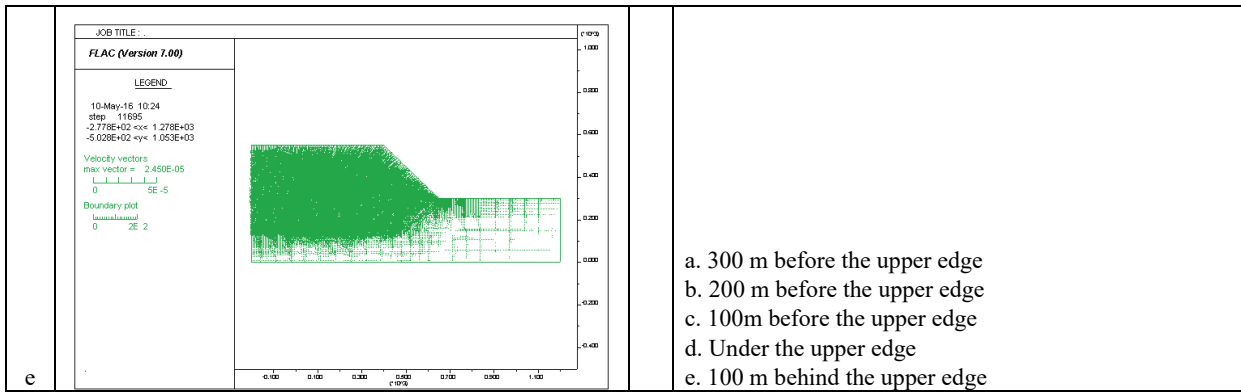


Fig. 16. Velocity vectors at particular stages of the longwall operation proceeding from the right side towards the lower edge of slope (measured point is the face of the longwall panel)

**Case III:** Longwall operation proceeds from the right side towards the lower edge of the open pit slope

In this case, vertical displacements begin to increase significantly, when the longwall face is located approx. 100 m before the lower edge of the slope (Fig. 17). Further progress of the longwall results in the situation that after reaching 100 m behind the lower edge of the slope,

the vertical displacement rises to 1.85 m at the pit floor and 1.7 m at the lower edge of the slope. The horizontal displacements are directed towards the pit floor, which can generate an activation of landslide. The value of the horizontal displacements in the lower part of the slope is approximately 1.0 m (Fig 18).

The plasticity indicator shows where the failures have formed (Fig. 19b). It signals the possibility of slope landslide after the longwall face, reaching 100 m behind

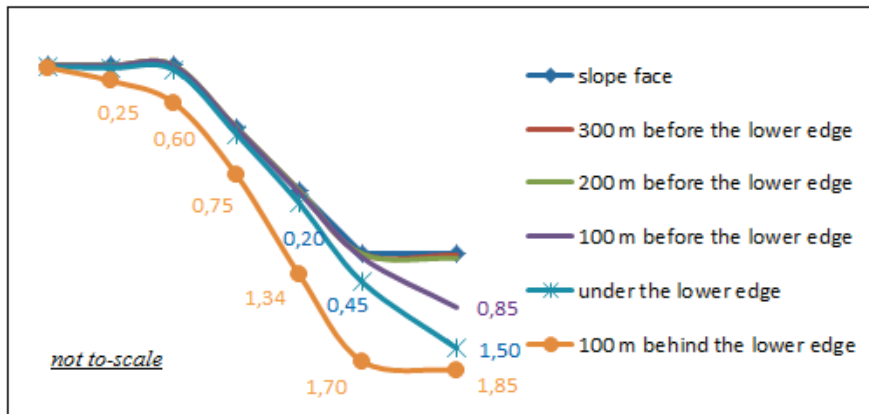


Fig. 17. Vertical displacement of slope face when the longwall operation proceeds from the right side toward the lower edge of slope (measured point is the face of the longwall panel)

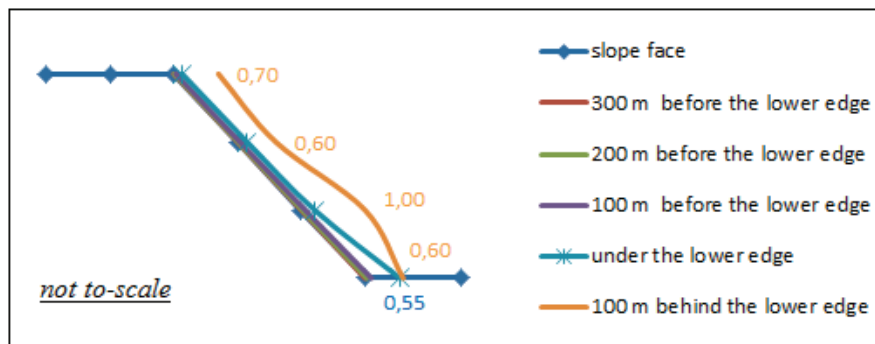


Fig. 18. Horizontal displacement of slope face when the longwall operation proceeds from the right side toward the lower edge of slope (measured point is the face of the longwall panel)

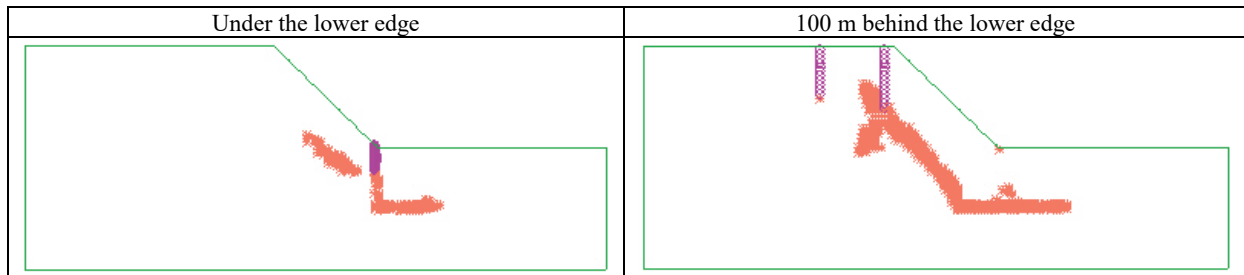


Fig. 19. Plastic indicator at particular stages of the longwall operation proceeding from the right side towards the lower edge of slope (measured point is the face of the longwall panel)  
(Note: violet color shows tension failure while red color shows shear failure)

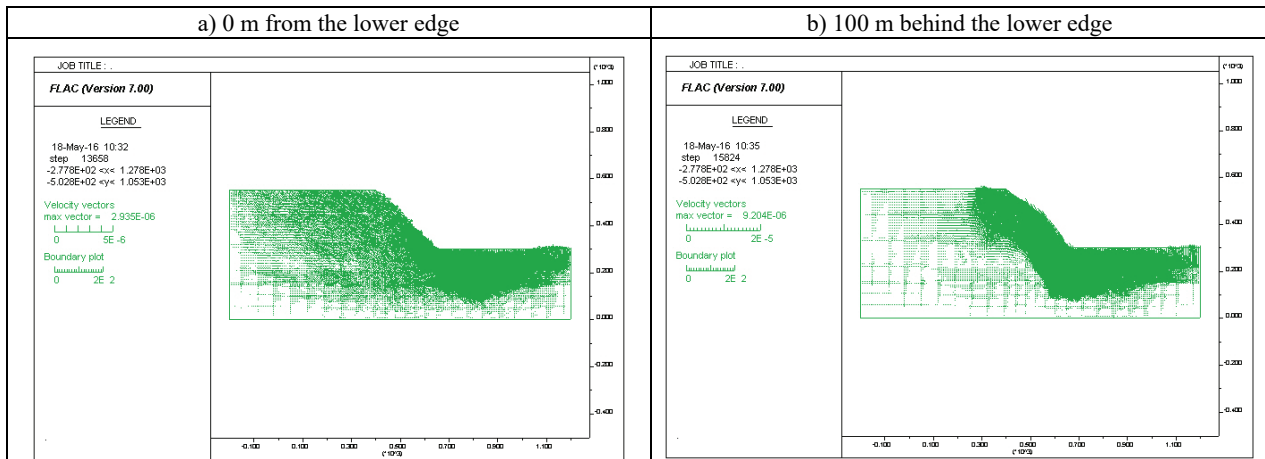


Fig. 20. Velocity vectors at particular stages of the longwall operation proceeding from the right side toward the lower edge of slope (measured point is the face of the longwall panel)

the lower edge. Further process of longwall operation could cause the failures by tension and shear in the upper part of the slope and, hence, the loss of stability.

Maximum velocity vectors are 3 times greater when the exploitation proceeds from the lower edge (Fig. 20a) to 100 m behind the lower edge in the direction of the slope (Fig. 20b). This indicates the possibility of failures in the face slope. The direction of the velocity vectors shown is unfavorable from the point of view of slope stability.

## 6. CONCLUSIONS

Based on the analysis performed by using numerical program FLAC 2D for underground mining operating in the area of open pit slope, for the geological and mining conditions of Quang Ninh coal basin in Vietnam, the following conclusions may be drawn:

- The zone located at a distance from 200 meters before the upper edge and 200 m before the lower edge of the slope is strongly affected by underground

mining operation, hence it is not recommended to operate underground workings in this zone;

- For the operation of longwall panel with the caving method, performed from the left side toward the upper edge of the slope, the operation can be carried out up to 100 meters before the upper edge, whereas in the case of the direction of the longwall panel performed from the right side toward the lower edge, the operation should be completed around 100 m before the bottom edge of the slope;
- In realistic conditions there are many other factors affecting slope stability, e.g., underground water, tectonic disturbance, presence of weak layers of rock, heterogeneity of rock mass and change of rock mass properties due to underground operation. It is necessary to take all those factors into account for further studies of interaction between UG and OP.
- In general, a 2D model indicates the impact of underground mining on slope stability. However, the rock mass structure and geometry are spatial and complex, therefore it is also necessary to use a three-dimensional numerical modeling for certain cases.



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